

Are you Ready for Calculus 3 (Multivariable Calculus)?

1. Find all of the discontinuities of $f(x)$, and identify the type of discontinuity.

$$f(x) = \frac{x^2 - 1}{x^2 - 7x + 6}$$

For #2-6, evaluate the limit

2. $\lim_{n \rightarrow \infty} \frac{3n^3 - 5n}{1 - 2n^2 + n^3}$

3. $\lim_{x \rightarrow 0} \frac{(x-5)^2 - 25}{x} =$

4. $\lim_{x \rightarrow 0} \frac{e^{3x} - e^{5x}}{x}$

5. $\lim_{h \rightarrow 0} \frac{\sqrt{5+h} - \sqrt{5}}{h} =$

6. $\lim_{x \rightarrow 0} \frac{\sin 3x}{3x^2 + 6x}$

For #7-9, find the derivative

7. $y = e^{2x} - \ln x^2 + \cos^2 4x$

8. $y = x^3 e^{2x} - \sec 5x$

9. $y = \ln(\sin 2x)$

10. Find the local and absolute extrema for $f(x) = 2x^3 + 9x^2 + 12x - 1$ on $[-3, 2]$.

For #11-14, evaluate the integral

11. $\int (\cos 2x) e^{\sin 2x} dx$

12. $\int_1^2 (x e^{6x}) dx$

13. $\int \frac{x+2}{x^2+4x+9} dx$

14. $\int_1^3 \left(\frac{x^2-1}{x+1} \right) dx$

15. The function f is continuous on the closed interval $[2,8]$ and has values that are given in the table. Using three subintervals, approximate the right endpoint, left endpoint, and trapezoid approximation of $\int_2^8 f(x)dx$?

x	2	5	7	8
$f(x)$	10	30	40	20

16. Find the area of the region between the graphs of $y = \sin^2 x$ and $y = -x$ from $x = 0$ to $x = 2$

17. The length of the curve $y = x^3$ from $(0,0)$ to $(1,1)$

18. If the region enclosed by the y -axis, the line $y=2$, and the curve $y = \sqrt{x}$ is revolved about the y -axis, find the volume of the solid generated.

19. Identify the Conic Section

(a) $x^2 + y^2 - 2x + 6y + 9 = 0$

(b) $x^2 - 25y^2 - 14x + 100y - 76 = 0$

(c) $3(y-2) = 2(x-15)$

(d) $x^2 + 36y^2 - 16x - 72y + 64 = 0$

(e) $x^2 + 4x - 8y + 12 = 0$

20. Change from Rectangular form to Polar form

(a) $xy = -4$

(b) $x^2 + y^2 - 3x = 10y$

21. Change from Polar form to Rectangular form

(a) $r = 4 \csc \theta$

(b) $r = 6 \cos \theta - 2 \sin \theta$

22. Eliminate the parameter t and write the equation in rectangular form

(a) $x = 2t^2 + 3, y = t - 1$

(b) $x = 3 \cos t, y = 3 \sin t$